

Soft X-ray Absorption and Resonant Scattering

1. Soft X-ray Absorption

Basic

Experimental Setup

Applications

- Chemical analysis

- Orbital polarization
- Magnetic Circular Dichroism

2. Resonant Soft X-ray Scattering

Introduction

- Basic of resonant X-ray scattering Examples:
- Magnetic Transition of a Quantum Multiferroic LiCu₂O₂



Interaction of photons with matter:

Photoelectric effect Photoabsorption Scattering/diffraction



- lattice structure: arrangement of atoms
- electronic states
- magnetic order
- excitations (electronic states or phonons)



Absorption probability:

$$W = \frac{2\pi}{\hbar} |M_{ij}|^2 \delta(\hbar \omega - E_f + E_i) \qquad M_{ij} \propto \langle f | \mathbf{\epsilon} \cdot \hat{\mathbf{r}} | i \rangle$$

Dipole transition

Absorption probability:
$$W = \frac{2\pi}{\hbar} |M_{ij}|^2 \delta(\hbar\omega - E_f + E_i)$$
 $M_{ij} \propto \langle f | \mathbf{\epsilon} \cdot \hat{\mathbf{r}} | i \rangle$
 $\mathbf{\epsilon} \cdot \hat{\mathbf{r}} = e_x \sin \theta \cos \phi + e_y \sin \theta \sin \phi + e_z \cos \theta$
 $\hat{\mathbf{r}} = (\sin \theta \cos \phi, \sin \theta \sin \phi, \cos \theta)$
 $\cos \theta = \sqrt{\frac{4\pi}{3}} Y_{1,0}(\theta, \phi)$ $\sin \theta \cdot e^{\pm i\phi} = \mp \sqrt{\frac{8\pi}{3}} Y_{1,\pm 1}(\theta, \phi)$ $\langle \Psi_{I',m'} | Y_{1,\pm 1} | \Psi_{I,m} \rangle \neq 0$
 $\mathbf{\epsilon} \cdot \hat{\mathbf{r}} = \sqrt{\frac{4\pi}{3}} (\frac{-\varepsilon_x + i\varepsilon_y}{\sqrt{2}} Y_{1,1} + \frac{\varepsilon_x + i\varepsilon_y}{\sqrt{2}} Y_{1,-1} + \varepsilon_z Y_{1,0})$ when
Dipole allowed transition $2\mathbf{p} \rightarrow 3\mathbf{d}$: $\Delta m \equiv m' - m = \pm 1$

$$M_{ij} \propto \left\langle 2p^5 3d^{n+1} \Big| \mathbf{\epsilon} \cdot \mathbf{r} \Big| 2p^6 3d^n \right\rangle$$

L. circularly polarized: $\Delta m_l = +1$ ($\therefore Y_{1,1}$) **R. circularly polarized:** $\Delta m_l = -1$ ($\therefore Y_{1,-1}$)

Dipole allowed transitions :

- $1s \rightarrow np$ K-edge XAS can be accurately described with single-particle methods.
- $2p \rightarrow 3d$ L-edge XAS: the single-particle approximation breaks down and the pre-edge structure is affected by the core hole wave function. The multiplet effect exists.



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Each element has specific absorption energies. "finger print" \rightarrow element specific spectroscopy



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Measurement of Soft X-ray Absorption



Photoexcitation and Relaxation





Measurement of Soft X-ray Absorption



L-edge XAS provides information on the chemical state, orbital symmetry, and spin state of materials.

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Polarization of Synchrotron Radiation



Soft X-Ray Magnetic Circular Dichroism in Absorption



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Soft X-Ray Magnetic Circular Dichroism in Absorption



Soft X-Ray Magnetic Circular Dichroism in Absorption

Soft X-ray MCD in absorption provides a unique means to probe:

element-specific magnetic hysteresis orbital and spin moments magnetic coupling.

There are two ways to obtain a MCD spectrum:

- 1) Fixing M, measure XAS with left and right circular lights.
- 2) Fixing the helicity of light, measure XAS with two opposite directions of M.



Element-Specific Magnetic Hysteresis Measurements

A New Technique for Studying Interlayer Magnetic Coupling

Ferromagnetism in one-dimensional monatomic metal chains

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Nature 416, 301 (2001)

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Two-dimensional systems, such as ultrathin epitaxial films and superfattices, display magnetic properties distinct from bulk materials¹. A challenging aim of current research in magnetism is to explore structures of still lower dimensionality^{1–6}. As the dimensionality of a physical system is reduced, magnetic ordering tends to decrease as fluctuations become relatively more important⁷. Spin lattice models predict that an infinite one-dimensional linear chain with short-range magnetic interactions spontaneously breaks up into segments with different orientation of the magnetization, thereby prohibiting long-range ferromagnetic order at a finite temperature^{1–9}. These models, however, do not take into account kinetic barriers to reaching equilibrium or interactions with the substrates that support the one-dimensional manostructures. Here we demonstrate the existence of both short- that the monatomic chains consist of thermally fluctuating segments of ferromagnetically coupled atoms which, below a threshold temperature, volve into a ferromagnetic long-range ordered state owing to the presence of anisotropy barriers. The Co chains are characterized by large localized orbital moments and correspondingly large magnetic anisotropy energies compared to two-dimensional films and bulk Co.





Figure 1 STM topographs of the Pt(997) surface. **a**, Periodic step structure (each white line represents a single step). The surface has a 6.45° miscut angle relative to the (111) direction; repulsive step interactions result in a narrow terrace width distribution centred at 20.2Å with 2.9Å standard deviation. **b**, Co monatomic chains decorating the Pt step edges (the vertical dimension is enhanced for better contrast). The monatomic chains are obtained by evaporating 0.13 monolayers of Co onto the substrate held at T = 260 K and previously cleaned by ion sputtering and annealing cycles in ultrahigh vacuum (UHV). The chains are linearly aligned and have a spacing equal to the terrace **yigth**.



Figure 2 Co X-ray absorption spectra for parallel (μ_+) and antiparallel (μ_-) direction of light polarization and field-induced magnetization. The dichroism signal ($\mu_+ - \mu_-$) is obtained by subtraction of the absorption spectra in each panel and normalization to the L₂ peak. **a**, Monatomic chains; **b**, one monolayer; **c**, thick Co film on Pt(997). The sample was mounted onto a UHV variable-temperature insert that could be rotated with the respect to the direction of the external magnetic field applied parallel to the incident photon beam. Spectra were recorded in the electron-yield mode at T = 10 K and

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$$\frac{d\sigma}{d\Omega} \propto \left| f_q \right|^2$$

Fourier transform of charge distribution.

Resonant scattering

As the photon energy $\hbar \omega$ approaches the binding energy of one of the core-level electrons,



Advantage of Resonant Soft X-ray Scattering



Resonant X-ray magnetic scattering

electric dipole transitions

Hannon et al., PRL(1988)



As a result of spin-orbit and exchange interactions, magnetic ordering manifests itself in resonant scattering.

Resonant soft x-ray magnetic scattering:

•Cross section comparable to that of neutron scattering.

•Good q resolution ($\Delta q < 0.0005 \text{ Å}^{-1}$)

•Spectroscopic information.

•Limited to a small k space, less bulk sensitive.

Setup of Soft X-ray Scattering



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Magnetism: ordering of spins



Magnetization can be induced by H field

Ferroelectricity: polar arrangement of charges



Electric polarization can be induced by E field

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Magnetoelectric effect

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Induction of magnetization by an electric field; induction of polarization by a magnetic field.

- first presumed to exist by Pierre Curie in 1894 on the basis of symmetry considerations

Multiferroics: materials exhibiting ME coupling Cr₂O₃ BiMnO₃ BiFeO₃ However, the effects are typically too small to be useful in applications!

Two contrasting order parameters

Magnetization: time-reversal symmetry broken



Polarization: inversion symmetry broken

$$\vec{r} \Rightarrow -\vec{r}: \ \vec{P} \Rightarrow -\vec{P}, \ \vec{M} \Rightarrow \vec{M}$$

 $\vec{P} = q\vec{r}$

Recently discovery in the coexistence and gigantic coupling of antiferromagnetism and ferroelectricity in frustrated spin systems such RMnO₃ and RMn₂O₅

(R=Tb, Ho , ...) _{ть}

TbMnO₃: Kimura et al., Nature 426, 55, (2003) TbMn₂O₅: Hur et al., Nature 429, 392 (2004)



revived interest in "multiferroicity"

Magnetism and ferroelectricity coexist in materials called "multiferroics."



• Ferroelectricity is induced magnetism.



Quantum multiferroic magnet LiCu₂O₂



orthorhombic, *Pnma* a=5.734 Å, b=2.856 Å, c=12.415 Å

Qausi-1D spin ½ chain: •Characterization of the ground state? •Multiferroicity (Park et al. PRL98, 057601; Seki et al., PRL (2008); cond-mat 0810.2533

















Above T_N, in-plane correlation

$$\xi(\boldsymbol{T}) \propto \mathrm{e}^{2\pi\rho_S/k_BT}$$

2D renormalized classical behavior

average J ~ 4.25 meV

- The ground state of LiCu₂O₂ exhibits a long range AFM ordering.
- •The spin coupling along the c axis is essential for inducing P.

Thank you!

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Appendix: Basic of Magnetic Circular Dichroism in X-ray Absorption



Considering L-edge $2p_{3/2} \rightarrow 3d$ absorption, and ignoring the spin-orbit interaction

$$\sigma \propto \left| \langle l, m_l | \boldsymbol{\epsilon} \cdot \hat{\mathbf{r}} | j, m_j \rangle \right|^2$$

$$\hat{\mathbf{r}} = (\sin \theta \cos \phi, \sin \theta \sin \phi, \cos \theta)$$

$$\boldsymbol{\epsilon} \cdot \hat{\mathbf{r}} = e_x \sin \theta \cos \phi + e_y \sin \theta \sin \phi + e_z \cos \theta$$

$$\cos \theta = \sqrt{\frac{4\pi}{3}} Y_{1,0}(\theta, \phi) \quad \sin \theta \cdot e^{\pm i\phi} = \mp \sqrt{\frac{8\pi}{3}} Y_{1,\pm 1}(\theta, \phi)$$

$$\boldsymbol{\epsilon} \cdot \hat{\mathbf{r}} = \sqrt{\frac{4\pi}{3}} (\frac{-\epsilon_x + i\epsilon_y}{\sqrt{2}} Y_{1,1} + \frac{\epsilon_x + i\epsilon_y}{\sqrt{2}} Y_{1,-1} + \epsilon_z Y_{1,0})$$

$$\sigma_{\pm} \propto R(r)^2 \cdot \left| \langle Y_{lm} | \frac{\boldsymbol{\epsilon}_x \mp i\boldsymbol{\epsilon}_y}{\sqrt{2}} Y_{1,\pm 1} | j, m_j \rangle \right|^2$$

$$\sigma_{\pm} \propto \left| \langle Y_{2,2} | \frac{\boldsymbol{\epsilon}_x - i\boldsymbol{\epsilon}_y}{\sqrt{2}} Y_{1,1} | j = \frac{3}{2}, m_j = \frac{1}{2} \rangle \right|^2 = \frac{1}{3}$$

$$\because \langle Y_{2,2} | Y_{1,1} | j = \frac{3}{2}, m_j = \frac{1}{2} \rangle = \sqrt{\frac{1}{3}} \langle Y_{2,2} | Y_{1,1} | j = \sqrt{\frac{1}{3}}$$

$$\sigma_{-} \propto \left| \langle Y_{2,0} | \frac{\boldsymbol{\epsilon}_x + i\boldsymbol{\epsilon}_y}{\sqrt{2}} Y_{1,-1} | j = \frac{3}{2}, m_j = \frac{1}{2} \rangle \right|^2 = \frac{1}{18}$$

$$\because \langle Y_{2,0} | Y_{1,-1} | j = \frac{3}{2}, m_j = \frac{1}{2} \rangle = \sqrt{\frac{1}{3}} \langle Y_{2,0} | Y_{1,-1} | Y_{1,1} \rangle = \sqrt{\frac{1}{18}}$$

$$m_{1} = 2 \qquad I \qquad 0 \qquad -I \qquad -2$$

$$L_{3} \qquad I/3 \qquad I/3 \qquad I/3 \qquad I/4 \qquad I/$$

Clesbsch-Gordan coefficients

$$Y_{lm} = \sum_{m_1m_2} (l_1m_1l_2m_2 \mid l, m)Y_{l_1m_1}Y_{l_2m_2}$$
$$Y_{l_1m_1}Y_{l_2m_2} = \sum_{l=l_1-l_2}^{l_1+l_2} (l_1m_1l_2m_2 \mid lm)Y_{lm}$$
$$Y_{l,1}Y_{l,1} = Y_{2,2} \qquad Y_{l,-1}Y_{l,1} = \sqrt{\frac{1}{6}}Y_{12,0} + \dots$$

$$\sigma \propto \left| \langle l, m_l | \mathbf{\epsilon} \cdot \hat{\mathbf{r}} | j, m_j \rangle \right|^2$$

$$\mathbf{\epsilon} \cdot \hat{\mathbf{r}} = \sqrt{\frac{4\pi}{3}} \left(\frac{-\epsilon_x + i\epsilon_y}{\sqrt{2}} Y_{1,1} + \frac{\epsilon_x + i\epsilon_y}{\sqrt{2}} Y_{1,-1} + \epsilon_z Y_{1,0} \right)$$

$$\sigma_{\pm} \propto R(r)^2 \cdot \left| \langle Y_{lm} | \frac{\epsilon_x \mp i\epsilon_y}{\sqrt{2}} Y_{1,\pm 1} | j, m_j \rangle \right|^2$$

$$\sigma_{\pm} \propto \left| \langle Y_{2,1} | \frac{\epsilon_x - i\epsilon_y}{\sqrt{2}} Y_{1,1} | j = \frac{3}{2}, m_j = -\frac{1}{2} \rangle \right|^2 = \frac{1}{3}$$

$$\because \langle Y_{2,1} | Y_{1,1} | j = \frac{3}{2}, m_j = -\frac{1}{2} \rangle = \sqrt{\frac{3}{3}} \langle Y_{2,1} | Y_{1,1} | Y_{1,0} \rangle = \sqrt{\frac{1}{3}}$$

$$Y_{1,1} Y_{1,0} = \sqrt{\frac{1}{2}} Y_{2,1} + \dots$$

$$\sigma_{-} \propto \left| \langle Y_{2,-1} | \frac{\epsilon_x + i\epsilon_y}{\sqrt{2}} Y_{1,-1} | j = \frac{3}{2}, m_j = -\frac{1}{2} \rangle \right|^2 = \frac{1}{3}$$

$$\because \langle Y_{2,-1} | Y_{1,-1} | j = \frac{3}{2}, m_j = -\frac{1}{2} \rangle = \sqrt{\frac{2}{3}} \langle Y_{2,-1} | Y_{1,-1} | Y_{1,0} \rangle = \sqrt{\frac{1}{3}}$$

$$Y_{1,-1} Y_{1,0} = \sqrt{\frac{1}{2}} Y_{2,-1} + \dots$$

$$m_{1} = 2 \qquad I \qquad 0 \qquad -I \qquad -2$$

$$L_{3} \qquad I/3 \qquad I/3 \qquad I/4 \qquad I/4 \qquad I/1 \qquad I/4 \qquad I/$$

Clesbsch-Gordan coefficients

$$Y_{lm} = \sum_{m_1m_2} (l_1m_1l_2m_2 \mid l, m)Y_{l_1m_1}Y_{l_2m_2}$$
$$Y_{l_1m_1}Y_{l_2m_2} = \sum_{l=|l_1-l_2|}^{l_1+l_2} (l_1m_1l_2m_2 \mid lm_2)Y_{lm_1}$$

$$\begin{split} m_{i} &= 2 \quad I \quad 0 \quad -I \quad -2 \\ \uparrow \quad 1 \quad 1/3 \quad 1/18 \\ L_{3} \\ m_{j} &= 3/2 \\ \sigma_{+} &\propto R(r)^{2} \cdot \left| \left\langle Y_{lm} \left| \frac{\mathcal{E}_{x} - i\mathcal{E}_{y}}{\sqrt{2}} Y_{1,1} \right| j, m_{j} \right\rangle \right|^{2} \\ \sigma_{+} &\propto \left| \left\langle Y_{2,2} \right| \frac{\mathcal{E}_{x} - i\mathcal{E}_{y}}{\sqrt{2}} Y_{1,1} \right| j = \frac{3}{2}, m_{j} = \frac{3}{2} \right\rangle \right|^{2} = 1 \\ & \because \left\langle Y_{2,2} \right| Y_{1,1} \left| j = \frac{3}{2}, m_{j} = \frac{3}{2} \right\rangle = \left\langle Y_{2,1} \right| Y_{1,1} \left| Y_{1,1} \right\rangle = 1 \\ \sigma_{+} &\propto \left| \left\langle Y_{2,1} \right| \frac{\mathcal{E}_{x} - i\mathcal{E}_{y}}{\sqrt{2}} Y_{1,1} \right| j = \frac{3}{2}, m_{j} = \frac{1}{2} \right\rangle \right|^{2} = \frac{1}{3} \\ & \because \left\langle Y_{2,1} \right| Y_{1,1} \left| j = \frac{3}{2}, m_{j} = \frac{1}{2} \right\rangle = \sqrt{\frac{2}{3}} \left\langle Y_{2,1} \right| Y_{1,1} \left| Y_{1,0} \right\rangle = \sqrt{\frac{1}{3}} \\ & Y_{1,1}Y_{1,0} = \sqrt{\frac{1}{2}} Y_{2,1} + \dots \\ \sigma_{+} &\propto \left| \left\langle Y_{2,0} \right| \frac{\mathcal{E}_{x} - i\mathcal{E}_{y}}{\sqrt{2}} Y_{1,1} \right| j = \frac{3}{2}, m_{j} = \frac{-1}{2} \right\rangle \right|^{2} = \frac{1}{18} \\ & \because \left\langle Y_{2,0} \right| Y_{1,1} \left| j = \frac{3}{2}, m_{j} = \frac{1}{2} \right\rangle = \sqrt{\frac{1}{3}} \left\langle Y_{2,0} \right| Y_{1,1} \left| Y_{1,-1} \right\rangle = \sqrt{\frac{1}{18}} \\ & Y_{1,1}Y_{1,-1} = \sqrt{\frac{1}{6}} Y_{2,0} + \dots \end{split}$$

$$Y_{lm} = \sum_{m_1m_2} (l_1m_1l_2m_2 \mid l, m)Y_{l_1m_1}Y_{l_2m_2}$$
$$Y_{l_1m_1}Y_{l_2m_2} = \sum_{l=|l_1-l_2|}^{l_1+l_2} (l_1m_1l_2m_2 \mid lm)Y_{lm}$$
$$Y_{l_1l_1} = Y_{2,2} \qquad Y_{l_1-l_1}Y_{l_1l_1} = \sqrt{\frac{1}{6}}Y_{32,0} + \dots$$

X-ray magnetic scattering

